

Assignment-2

Shanoob-m

Q) Drive the equation of motion and maximum tractive effort for a car inclined at an angle θ . also give the expression of maximum gradability for a 4 wheel drive?

Ans) where,

w = weight of the car

CG = centre of gravity

f = max^m forward acceleration

R_f & R_r = Rear & front wheel

R_R & R_F = Total normal reaction at front and rear wheel

h = height from CG to road surface.

$$\text{If } = \text{Inertia force} = m \cdot f - w \sin \theta$$
$$m \cdot f - m g \sin \theta = \frac{w}{g} \cdot f - w \sin \theta \quad \text{--- (1)}$$

$$\Sigma v = 0 \quad \text{--- (2)}$$

$$\Sigma H = 0 \quad \text{--- (3)}$$

In case of (2)

$$w \cos \theta = R_f + R_r \quad \text{--- (4)}$$

In case of (3)

$$R_f = \frac{w}{g} \cdot f + w \sin \theta$$

$$\mu R_f = \frac{w}{g} \cdot f + w \sin \theta$$

$$R_f = \frac{w}{g} \cdot f + \frac{w}{\mu} \sin \theta \quad \text{--- (5)} \quad \frac{w}{\mu} \left(\frac{f}{g} + \sin \theta \right)$$

Taking moment.

$$R_f \times b + \left(\frac{w}{g} \cdot f + w \sin \theta \right) h = w \cos \theta \times l$$

$$\left(\frac{w}{g} \cdot \frac{f}{\mu} + \frac{w}{\mu} \sin \theta \right) b + \left(\frac{w}{g} \cdot f + w \sin \theta \right) h = w \cos \theta \cdot l$$

$$\left(\frac{f}{g \mu} + \frac{\sin \theta}{\mu} \right) b + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$\frac{b}{\mu} \left(\frac{f}{g} + \sin \theta \right) + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$\left(\frac{f}{g} + \sin \alpha\right) = \frac{\cos \alpha \cdot l}{\left(\frac{b}{\mu} + h\right)} \quad \text{--- (8)}$$

$$\frac{f}{g} = \frac{\cos \alpha \cdot l}{\frac{b}{\mu} + h} - \sin \alpha$$

$$f = g \left(\frac{\cos \alpha \cdot l}{\left(\frac{b}{\mu} + h\right)} - \sin \alpha \right) \quad \text{--- (9)}$$

$$R_f = \frac{w}{\mu} \times \frac{\cos \alpha \cdot l}{\left(\frac{b}{\mu} + h\right)} = \frac{w \cos \alpha \cdot l}{b + \mu h}$$

$$\begin{aligned} R_R &= w \cos \alpha - R_f \\ &= w \cos \alpha - \frac{w}{\mu} \frac{\cos \alpha \cdot l}{\left(\frac{b}{\mu} + h\right)} \\ &= w \cos \alpha \left[1 - \frac{l}{(b + \mu h)} \right] \end{aligned}$$

$$= w \cos \alpha \cdot \left[\frac{b + \mu h - l}{b + \mu h} \right]$$

$$F_f = \mu R_f = \mu \times \left[\frac{w \cos \alpha \cdot l}{b + \mu h} \right]$$

Four wheel drive

$$F = R_f + R_R = \mu R_R + \mu R_f$$

where, $E_v = 0$

$$w = R_f + R_R$$

$$E_H = 0$$

$$\begin{aligned} \left(\frac{w}{g}\right) f &= \mu R_R + \mu R_f \\ &= \mu (R_R + R_f) = \mu w \end{aligned}$$

$$\left(\frac{f}{g}\right) = \mu$$

$$w = R_R + R_f$$

$$\sum H = 0$$

$$\left(\frac{w}{g}\right) F = M_{RR} + M_{RL}$$

assuming slip occur at front wheel

where, first $R_F < R_R$

then, $\sum M_R = 0$

$$2 M_{RF} = \left(\frac{w}{g}\right) F$$

$$\underline{\underline{R_F b + \left(\frac{w}{g}\right) F h = w_1}}$$

2 Q) Consider a car with the following specifications that is parked on a level road. find the load on the front and rear axles
 $m = 1765 \text{ kg}$, $l = 2.84 \text{ m}$, $a_1 = 1.22 \text{ m}$, $a_2 = 1.62 \text{ m}$

A) load on front axles $= F_{AF} = mg \left(\frac{a_2}{l}\right)$ load on rear axles $= F_{AR} = mg \left(\frac{a_1}{l}\right)$	$m = 1765 \text{ kg}$ $l = 2.84 \text{ m}$ $a_1 = 1.22 \text{ m}$ $a_2 = 1.62 \text{ m}$
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$$\begin{aligned}
 F_{AF} &= mg \left(\frac{a_2}{l}\right) \\
 &= 1765 \times 9.8 \times \left(\frac{1.62}{2.84}\right) \\
 &= 17247 \times 0.570 = \underline{\underline{9866.59 \text{ N}}}
 \end{aligned}$$

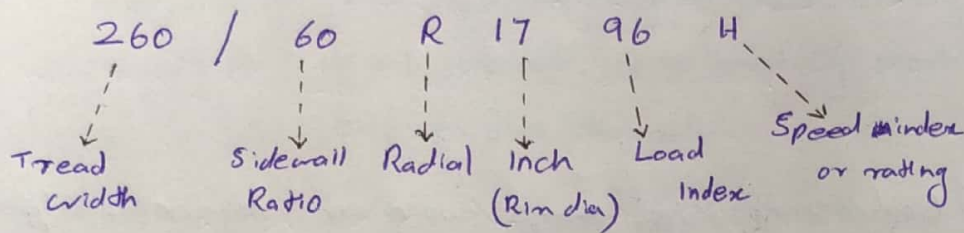
$$\begin{aligned}
 F_{AR} &= mg \left(\frac{a_1}{l}\right) \\
 &= 1765 \times 9.8 \times \left(\frac{1.22}{2.84}\right) = \underline{\underline{7430.40 \text{ N}}}
 \end{aligned}$$

$$\text{load on front axles} = \underline{\underline{9866.59 \text{ N}}}$$

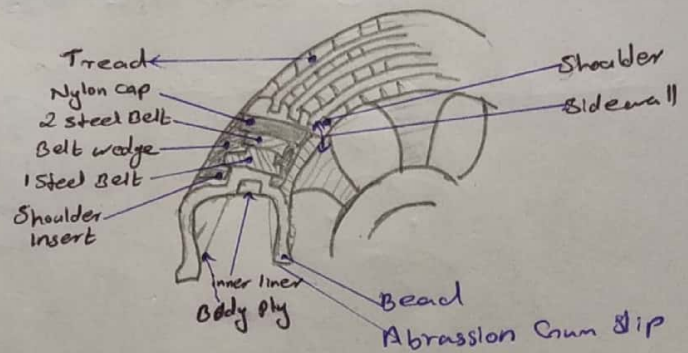
$$\text{load on Rear axles} = \underline{\underline{7430.40 \text{ N}}}$$

Q3 what are the different part of tires? Differentiate b/w types of tyre on the basis of their condition.

Ans) Tyre spec:-



- **Bead** :- It is a spring or spiral metal wire. the construction is similar to the clutch wire. (multiple clutch wire. in the form of single wire.



Dia of Bead < diameter of Rim

(slightly short) . that's why its works like spring. It act like an locking system of tyre with the rim.

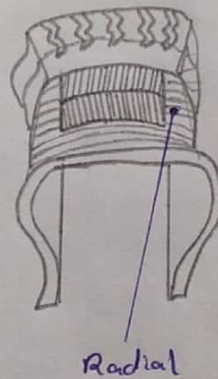
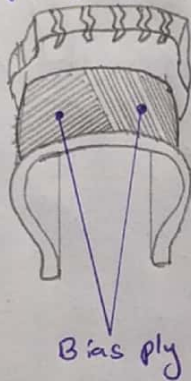
- **Bead Filler** → It act as an protector for the rubber from bead & avoid bead contact with the rubber.
- **Innerliner** :- It is a soft rubber compound. It helps from the leaking of air while puncture. It holds the air without escaping. the innerliner compound is same as that of the surgical gloves.
→ It is seen in the tubless & radial tyres.
- **Body ply** :- It is a soft rubber compound part but harder than the innerliner. the role of Body ply is to provide core strength. to the tyre.
→ It is a soft Rubber Compound with reinforcement. this could be anything for normal car Reinforcement will be Nylon, for heavy vehicle it is Kevlar & for sports car it will be carbon fiber.

→ Shoulder Insert :- the shoulder is the weakest point of tyre the joint tread & sidewall we use shoulder insert for giving strength.

→ Steel Belt :- It is provided to give more strength It will be made up of metal. It is basically provided to give Reinforcement to the tread.

→ Radial Cord Body :- It gives ~~tr~~ strength and transmits cornering forces from the tread to wheel

→ ~~Belt plys~~ :- ~~They are~~



- Bias ply tyre has a construction structure in which the ply cords extend to the beads and are laid at alternate angle substantially less than 90° to the centreline of the tread. It is cheap, weak traction, Less durable, Less fuel efficient & High load capacity.
- Radial tyre offer better performance, fuel consumption and comfort over bias tyre. although more expensive, savings on fuel and their durability make them more cost effective. has excellent traction, & only low load capacity.