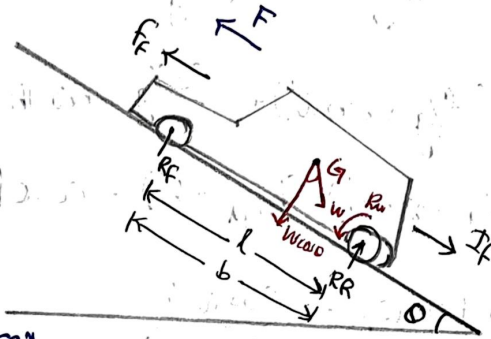


①

Derive the equation of motion and maximum tractive effort for a car inclined at angle θ . also give the expression of maximum gradeability for a 4 wheel drive.



W - weight of the car

b - wheel base

G - Center of gravity

R_f & R_r - Total normal reaction at front & rear wheels

h - height from road to G

F_f - Inertia force

F - max forward acceleration

F_f - max tractive effort

$$F_f = M \cdot F - W \sin \theta$$

$$= m \cdot f - m g \sin \theta$$

$$m = W/g$$

$$= W/g \cdot F - W \sin \theta \quad \text{--- (1)}$$

$$\sum V = 0 \quad \text{--- (2)}$$

$$\sum H = 0 \quad \text{--- (3)}$$

$$(2) \Rightarrow W \cos \theta = R_f + R_r \quad \text{--- (4)}$$

$$(3) \Rightarrow F_f = W/g \cdot F + W \sin \theta$$

$$\mu R_f = W/g \cdot F + W \sin \theta$$

$$R_r = W/g \cdot F + W/\mu \sin \theta \quad \text{---}$$

Taking moment about x

$$R_f \times b + (w/g \cdot f + \sin \theta) h = w \cos \theta \cdot l$$

$$\left(\frac{w}{g} \cdot \frac{l}{\mu} + \frac{w}{\mu} \sin \theta \right) b + \left(\frac{w}{g} f + w \sin \theta \right) h = w \cos \theta \cdot l$$

$$\Rightarrow \left(\frac{f}{g\mu} + \frac{\sin \theta}{\mu} \right) b + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$b/\mu \left(\frac{f}{g} + \sin \theta \right) + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$\left(\frac{f}{g} + \sin \theta \right) (b/\mu + h) = \cos \theta \cdot l$$

$$\left(\frac{f}{g} + \sin \theta \right) = \frac{\cos \theta \cdot l}{(b/\mu + h)}$$

$$\frac{F}{g} = \frac{\cos \theta \cdot l}{b/\mu + h} - \sin \theta$$

$$F = g \left[\left(\frac{\cos \theta \cdot l}{b/\mu + h} \right) - \sin \theta \right]$$

$$R_f = w/\mu \times \frac{\cos \theta \cdot l}{(b/\mu + h)} \quad \text{--- } \cancel{\sin \theta}$$

$$= \frac{w \cos \theta \cdot l}{b + \mu h}$$

$$R_R = w \cos \theta - R_f$$

$$= w \cos \theta - w/\mu \cdot \frac{\cos \theta \cdot l}{b/\mu + h}$$

$$= w \cos \theta \left[1 - \frac{l}{b + \mu h} \right]$$

$$= w \cos \theta \left[\frac{b + \mu h - l}{b + \mu h} \right]$$

$$F_f = \mu R_f = \mu \times \left(\frac{w \cos \theta \cdot l}{b + \mu h} \right)$$

Four wheel Drive

$$F = R_f + F_f = \mu R_R + \mu R_L$$

$$E_v = 0$$

$$W = R_f + R_R$$

$$E_\theta = 0$$

$$\begin{aligned} (w/g)F &= \mu R_R + \mu R_L = \mu (R_R + R_L) \\ &= \mu W \end{aligned}$$

$$F/g = \mu$$

$$E_v = 0$$

$$W = R_R + R_L$$

$$E_H = 0$$

$$(w/g)F = \mu R_R + \mu R_L$$

Assuming slip to occur at front wheel

$$\text{front } R_f \leq R_R \text{ then}$$

$$E_{MR} = 0 \quad 2\mu R_f = (w/g)F$$

$$\underline{R_f b + (w/g)F a = W l}$$

②

Consider Car with the following specification that is parked on a level road. find the load on the front and rear axles.

$$M = 1765 \text{ kg}$$

$$l = 2.84 \text{ m}$$

$$a_1 = 1.22 \text{ m}$$

$$a_2 = 1.62 \text{ m}$$

$$\text{Load on front axle } f_{AF} = mg \left(\frac{a_2}{l} \right)$$

$$= 1765 \times 9.8 \left(\frac{1.62}{2.84} \right)$$

$$f_{AF} = 9866.59 \text{ N}$$

$$\text{Load on front axels} = \underline{\underline{9866.59 \text{ N}}}$$

$$\text{Load on rear axels } f_{AR} = Mg \left(\frac{a_1}{l} \right)$$

$$= 1765 \times 9.8 \left[\frac{1.22}{2.84} \right]$$

$$= 7430.40 \text{ N}$$

$$\text{Load on rear axels} = \underline{\underline{7430.40 \text{ N}}}$$

③ What are the different ^{parts} ~~type~~ of tyres? Differentiate between types of tyres on the basis of their construction

① Side wall :- The area of a tyre from the bead to the tread. The side of the tyre is known as side wall. It forms a protective covering for the cord body.

② Tread :- Tread is the portion of tyre that comes in contact with the road surface. The tread compound and its design have to balance wear, traction, handling, fuel economy, resistance and other characteristics of the tyre.

③ Beads :- Beads hold the tyre to the rim or the outer edge of the wheel. They are made of copper, brass or boom plated high tensile steel wire wound into a rubber band. The bead prevents the tyre from sliding out of place when the wheel rolls.

④ Bead filler :- It is a rubber compound inside the tyre beads that provides stability to the lower side wall and bead area. The density and stiffness of a tyre's bead filler helps to determine tyre performance characteristics.

⑤ Radial cord body :- It gives the tyre strength and transmits cornering forces from the tread to the wheel. Rubber coated fabric.

Cord, called body ply. make up the cord body
body ply can be made of polyester,
rayon or nylon. polyester is most commonly
used

⑥ Belt plies - These are two or more strong layers
of cord just under the tread area of the
tire. The primary function of belt ply is
to provide strength and stability to the
tire tread. They play a role in improving
tire mileage, impact resistance and
traction. Steel is the most commonly
used cord material in belt plies.

⑦ Inner liner - It is a rubber compound bonded to the
inside of the cord body that retains air
under pressure. It has no cord reinforcement
and it functions like an inner tube. The
modern car tire ~~have~~ no longer have an inner
tube inside them.

Different types

Bias ply



- * The treads & side walls have the same carrying plys
- * Reduced traction
- * Nylon belts
- * Normal duty
- * Low cost and low life expectancy

Radial



- * Cord plies are arranged 90° to the direction of travel
- * Outstanding traction
- * Steel belts
- * Extreme duty
- * Expensive and long life expectancy