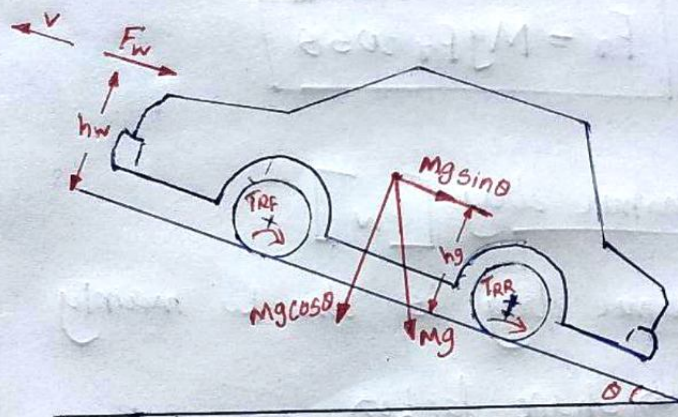


## Assignment-2

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Q1) Derive the equation of motion & maximum tractive effort for a car inclined at an angle  $\theta$ . Also give the effort for a maximum gradeability for a 4 wheel drive

a) for the Powertrain calculation at one angle  $\theta$  we have to find Rolling resistance, Aerodynamic drag, Grading resistance, and acceleration resistance



### Rolling resistance $[F_r]$

We can say that rolling resistance of vehicle is the sum of the front and back wheel resistance

i.e.,

$$F_r = F_{RF} + F_{RR}$$

but we take an  $F_r$  is a coefficient of  $F_r$  is a function of all physical contact parameters of tyre like eg: tyre material, road material etc...

Then at an angle  $\theta$

The Rolling resistance will be

$$F_r = P f_r \cos \theta$$

here

$$P = Mg$$

$m$  = mass of the vehicle

$P$  - Normal load acting on the centre of the radius of rolling wheel

hence equation becomes

$$F_r = Mg f_r \cos \theta$$

Aerodynamic drag  $[F_w]$

Aerodynamic drag is due to mainly

$\Rightarrow$  shape factor

$\Rightarrow$  skin effect

we know the equation for Aerodynamic drag considering the shape and Air property is,

$$F_w = \frac{1}{2} \rho A_f C_D V^2$$

where,  $\rho \Rightarrow$  density of air  $[kg/m^3]$

$A_f \Rightarrow$  vehicle frontal area  $[m^2]$

$V =$  vehicle speed  $[m/s]$

$C_D =$  drag coefficient.

Grading resistance  $[F_g]$ 

from the above figure,

when a vehicle goes up ~~top~~ or down a slope, its weight produces a component of force that is always act downwards. This opposes the forward motion

i.e

grading resistance

$$F_g = Mg \sin \theta$$

where,

$M$  = mass of vehicle  $[kg]$

$g$  = acceleration  $[m/s^2]$

$\theta$  = road angle

where

$$\theta = 0^\circ$$

$$F_g = 0 \text{ [minimum gradient]}$$

$$\text{where } \theta = 90^\circ \quad F_g = Mg$$

[maximum gradient]

Traction force  $(F_T)$ 

The tractive effort or force acting on front and rear wheel so, in the case of four wheel

Total traction force

$$F_T = F_{TF} + F_{TR}$$

↓  
for front

↘  
for rear wheel

We know Total resistance

~~F<sub>r</sub> + F<sub>w</sub> + F<sub>g</sub> + F<sub>a</sub>~~

$$F_{\text{resistance}} = F_r + F_w + F_g + F_a$$

here  $F_a$  = acceleration resistance

Traction force  $\rightarrow$  It is the force delivered by the motor or engine so that the vehicle can maintain grip on traction with surface

So we can derive the dynamic equation for resistance

$$M \cdot a = [F_{kF} + F_{kR}] - [F_r + F_w + F_g + F_a]$$

b) Gradeability :

It is measured either degree or Percentage. It depends on engine power, drive train type, gear ratio, weight of car's centre of gravity and traction

$$F = mg \sin \theta$$

$$\text{Total power} = \text{Total force} \times \text{speed}$$

$$\tan \theta \times 100 = \text{gradeability}$$

Q2) Consider a car with the following specifications that it is parked on a level road. Find the load on the front and rear axles  $m = 1765 \text{ kg}$   $l = 2.84 \text{ m}$   $a_1 = 1.22 \text{ m}$   $a_2 = 1.62 \text{ m}$

Ans) The front vehicle mass is

$$m_{VF} = mg \frac{a_2}{l}$$

$$= 1765 \times 9.81 \times \frac{1.62}{2.84}$$

$$= \underline{\underline{9876.59 \text{ N}}}$$

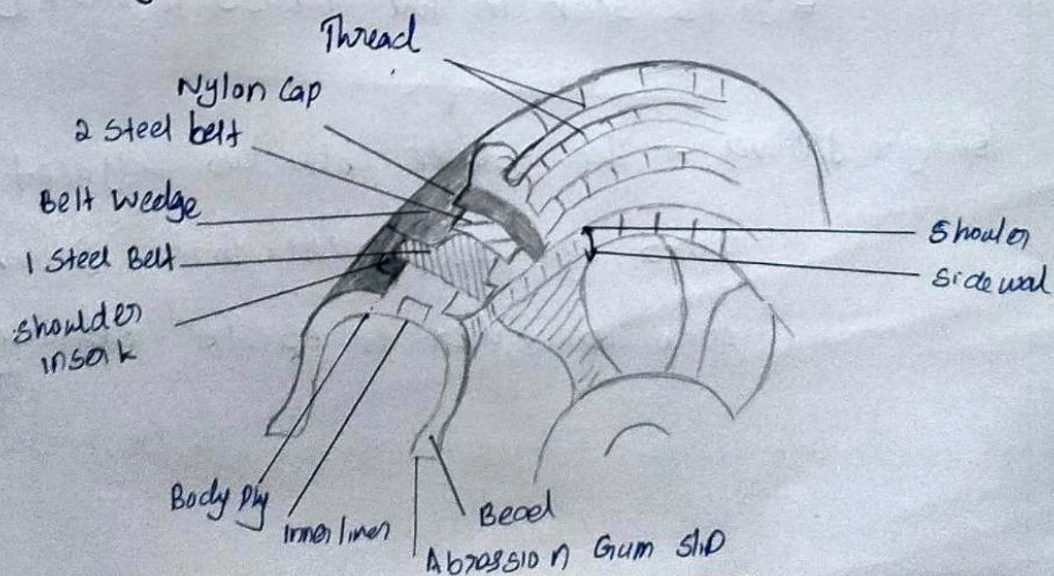
$$m_{VR} = mg \frac{a_1}{l}$$

$$= 1765 \times 9.81 \times \frac{\cancel{2.84}}{\cancel{2.84}} \times \frac{1.22}{2.84}$$

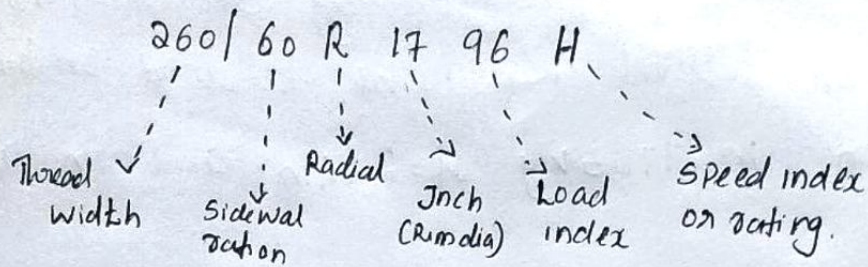
$$= \underline{\underline{7437.963 \text{ N}}}$$

Q3) what are the different parts of tyre? Differentiate b/w type of tyre on the basis of their conditions

Ans



## Tyre Specifications



main parts of the tyre shown in figs,

Bead  $\Rightarrow$  It is a spring or spiral metal wire. The construction is similar to the clutch wire

Dia of Bead < diameter of Rim

Bead filler  $\Rightarrow$  It acts as protection for the rubber from bead and avoid bead contact with the rubber

Inner liner  $\Rightarrow$  It is a main part of a tyre which resists the leakage of the air. It is made up of soft rubber compound. It helps the air without escaping. The inner compound is same as that of the surgical gloves

$\Rightarrow$  It is seen in the tubeless & radial tyres

~~Re~~ Tyre grooves  $\Rightarrow$  The space b/w two adjacent tread ribs are also called tread grooves. These allow water to escape effectively

Body Ply : It is a soft rubber compound part but harder than the inner liner the role of body ply is to provide core strength to the tyre.

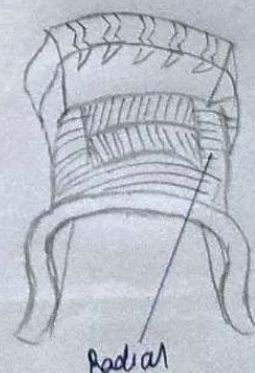
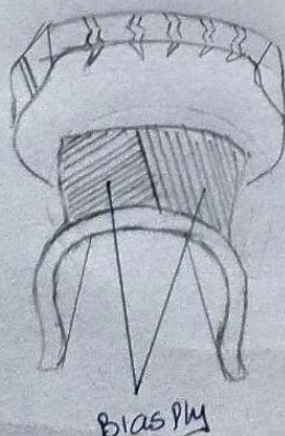
# It is soft rubber compound with reinforcement this could be anything for normal car reinforcement will nylon, for heavy vehicle it is kevlar or for sports car it will be carbon fiber.

Steel Belt : It is provided to give more strength it will be made of metal. It is basically provided to give reinforcement to the thread.

Shoulder Insert :- The weakest point of the tyre is shoulder joint thread or sidewall are use shoulder insert for giving strength.

Radial Cord Body :- It gives strength and transmits cornering forces from the thread to wheel.

Type of tyre based on their condition,



According to the conditions the tyres are mainly classified into two type

i) Bias Ply tyre

ii) Radial tyre

i) Bias Ply tyre

It has construction structure in which the ply cords extend to the beads and are laid at alternate angles substantially less than  $90^\circ$  to the centreline of the tread. It is cheap, weak traction, less durable less fuel efficient & high load capacity.

ii) Radial tyre

It offers better performance, fuel consumption and comfort over bias tyre. Although more expensive, saving on fuel and their durability make them more cost effective. It has excellent traction, & only low load capacity.