

Assignment - 2.

- Derive the equation of motion & maximum tractive effort for a car inclined at angle θ . Also give the expression of maximum gradeability for a 4 wheel drive.

W = weight of the car.

C_G = centre of gravity.

b = wheel base

F = maximum forward acceleration

F_F = maximum tractive effort.

R_R & R_F = Rear & Front wheel.

R_R & R_F = Total normal reaction at front & rear wheel.

h = height from C_G to road

I_F = Inertia force = $m \cdot f - W \sin \theta$.

$$= m \cdot f - \frac{W}{g} \sin \theta$$

$$= \frac{W}{g} f - W \sin \theta \quad \text{--- (1)}$$

$$\sum V = 0 \quad \text{--- (2)}$$

$$\sum H = 0 \quad \text{--- (3)}$$

using (2)

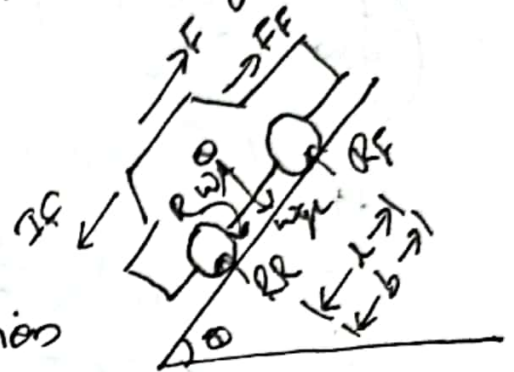
$$W \cos \theta = R_F + R_R \quad \text{--- (4)}$$

using (3)

$$F_F = \frac{W}{g} \cdot f + W \sin \theta.$$

$$\therefore R_F = \frac{W}{g} \cdot f + W \sin \theta.$$

$$R_F = \frac{W}{g} f + \frac{W}{g} \sin \theta \quad \text{--- (7)} \quad \frac{W}{g} \left\{ \frac{f}{g} + \sin \theta \right\}$$



Taking moment about y

$$R_F \cdot b + \left(\frac{\omega}{g} \cdot f + \omega \sin \theta \right) h = \omega \cos \theta \cdot l$$

$$\left(\frac{\omega}{g} \frac{b}{\mu} + \frac{\omega}{\mu} \sin \theta \right) b + \left(\frac{\omega}{g} f + \omega \sin \theta \right) h = \omega \cos \theta \cdot l$$

$$\left(\frac{f}{g\mu} + \frac{\sin \theta}{\mu} \right) b + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$\frac{b}{\mu} \left(\frac{f}{g} + \sin \theta \right) + \left(\frac{f}{g} + \sin \theta \right) h = \cos \theta \cdot l$$

$$\left(\frac{f}{g} + \sin \theta \right) \left(\frac{b}{\mu} + h \right) = \cos \theta \cdot l$$

$$\frac{f}{g} = \left(\frac{\cos \theta \cdot l}{\left(\frac{b}{\mu} + h \right)} \right) - \sin \theta$$

$$F = g \left[\frac{\cos \theta \cdot l}{\left(\frac{b}{\mu} + h \right)} - \sin \theta \right] \quad \text{--- (9)}$$

$$R_F = \frac{\omega}{\mu} \times \frac{\cos \theta \cdot l}{\left(\frac{b}{\mu} + h \right)} \quad \text{--- (10)}$$

$$= \frac{\omega \cos \theta \cdot l}{b + \mu h}$$

$$R_R = \omega \cos \theta - R_F = \omega \cos \theta - \frac{\omega}{\mu} \frac{\cos \theta \cdot l}{\left(\frac{b}{\mu} + h \right)}$$

$$= \omega \cos \theta \left[1 - \frac{1}{\left(\frac{b}{\mu} + h \right)} \right]$$

$$= \omega \cos \theta \left[\frac{b + \mu h - 1}{b + \mu h} \right]$$

$$F_F = \mu R_F = \mu \times \left(\frac{\omega \cos \theta \cdot l}{b + \mu h} \right)$$

Four wheel drive.

$$F = R_F + F_F = \mu R_R + \mu R_F$$

$$\Sigma V = 0$$

$$\omega = R_F + R_R$$

$$\Sigma H = 0$$

$$(\omega/g) F = \mu R_R + \mu R_F = \mu (R_R + R_F) = \mu \omega$$

$$(F/g) = \mu$$

$$\Sigma V = 0$$

$$\omega = R_R + R_F$$

$$\Sigma H = 0$$

$$(\omega/g) F = \mu R_R + \mu R_F$$

Assuming slip to occur at front wheels

First $R_F < R_R$ then

$$\Sigma MR = 0$$

$$2 \mu R_F = (\omega/g) F$$

$$\underline{\underline{R_F b + (\omega/g) F b = \omega l}}$$

2) Consider a car with the following specifications that is parked on a level road. Find the load on the front and rear axles. $m = 1765 \text{ kg}$, $l = 2.84 \text{ m}$, $a_1 = 1.22 \text{ m}$, $a_2 = 1.62 \text{ m}$.

$$M = 1765 \text{ kg}$$

$$l = 2.84 \text{ m}$$

$$a_1 = 1.22 \text{ m}$$

$$a_2 = 1.62 \text{ m}$$

$$\text{load on front axles} = F_{AF} = mg \left(\frac{a_2}{l} \right)$$

$$\text{load on rear axles} = F_{AR} = mg \left(\frac{a_1}{l} \right)$$

$$F_{AR} = mg \left(\frac{a_1}{l} \right) = 1765 \times 9.8 \times \left(\frac{1.22}{2.84} \right) = 17297 \times 0.429 = \underline{\underline{7430.40 \text{ N}}}$$

$$\text{load on rear axles} = \underline{\underline{7430.40 \text{ N}}}$$

$$F_{AF} = mg \left(\frac{a_2}{l} \right) = 1765 \times 9.8 \times \left(\frac{1.62}{2.84} \right) = 17297 \times 0.570 = \underline{\underline{9866.59 \text{ N}}}$$

$$\text{load on front axles} = \underline{\underline{9866.59 \text{ N}}}$$

3) what are the different parts of tires? Differentiate between types of tires on the basis of their construction.

Tyre parts

1. Beads

We'll start from the inside and Tyre beads hold tyre to the rim, or the outer edge of the wheel.

They are made of copper, brass, or bronze-plated high tensile steel wires wound into a rubber band. Tire beads prevent the tire from sliding out of place when the wheel rolls.

2. BEADS

Bead filler is a rubber compound inside the tire's beads. It provides stability to the lower sidewall and bead area. The density and stiffness of a tire's bead filler help to determine a tire's performance characteristics.

3. RADIAL CARDBODY

The cardbody gives the tire strength and transmits cornering forces from the tread to the wheel. Rubber coated fabric cord, called body plies, make up the card body. Body plies can be made of polyester, rayon or nylon. polyester is most commonly used.

4. INNER LINER

The inner liner is rubber compound bonded to the inside of the card body that retains air under pressure. It has no cord reinforcement, and it functions like an inner tube. That modern car tires no longer have inner tubes inside them. A tire's beads, bead filler and inner liner work together to hold air within the tire wall.

5. BELT PLIES

Belt plies are two or more strong layers of cord just under the tread area of the tire. The primary function of belt plies is to provide strength and stability to the tire tread. They play a role in improving tire mileage, impact resistance, and traction. Steel is the most common cord material used in belt plies.

6. SIDE WALL

The area of a tire from the bead to the tread. The side of the tire is called the sidewall. It forms a protective covering for the cord body.

7. TREAD

The tread is the portion of the tire that comes in contact with the road surface. The tread's compound and its design have to balance w. traction, handling, fuel economy, resistance and other characteristics of the tire.

BIAS TIRES

- Nylon Belts
- Standard duty
- Less Expensive
- low life expectancy

RADIAL TIRES.

- steel belts
- Severe/Extreme duty.
- More expensive
- long life expectancy.